# C-ID Descriptor Discrete Structures

## **Descriptor Details**

• Descriptor Title: Discrete Structures

• **C-ID Number**: 152

• Units: 3.0

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## **General Description**

This course is an introduction to the discrete structures used in Computer Science with an emphasis on their applications. Topics covered include: Functions, Relations and Sets; Basic Logic; Proof Techniques; Basics of Counting; Graphs and Trees; and Discrete Probability.

## **Prerequisites**

**COMP 122** 

## **Corequisites**

No information provided

#### **Advisories**

No information provided

#### **Content**

- I. Functions, Relations and Sets
  - 1. Functions (surjections, injections, inverses, composition)
  - 2. Relations (reflexivity, symmetry, transitivity, equivalence relations)
  - 3. Sets (Venn diagrams, complements, Cartesian products, power sets)

- 4. Pigeonhole principles
- 5. Cardinality and countability

#### II. Basic Logic

- 1. Propositional logic
- 2. Logical connectives
- 3. Truth tables
- 4. Normal forms (conjunctive and disjunctive)
- 5. Validity
- 6. Predicate logic
- 7. Universal and existential quantification
- 8. Modus ponens and modus tollens
- 9. Limitations of predicate logic

#### III. Proof Techniques

- 1. Notions of implication, converse, inverse, contrapositive, negation, and contradiction
- 2. The structure of mathematical proofs
- 3. Direct proofs
- 4. Proof by counterexample
- 5. Proof by contradiction
- 6. Mathematical induction
- 7. Strong induction
- 8. Recursive mathematical definitions
- 9. Well orderings

#### IV. Basics of Counting

- 1. Counting arguments
- 2. Sum and product rule
- 3. Inclusion-exclusion principle
- 4. Arithmetic and geometric progressions
- 5. Fibonacci numbers
- 6. The pigeonhole principle
- 7. Permutations and combinations
- 8. Basic definitions
- 9. Pascal's identity
- 10. The binomial theorem
- 11. Solving recurrence relations
- 12. Common examples

- 13. The Master theorem
- V. Graphs and Trees
  - 1. Trees
  - 2. Undirected graphs
  - 3. Directed graphs
  - 4. Spanning trees/forests
  - 5. Traversal strategies
- VI. Discrete Probability
  - 1. Finite probability space, probability measure, events
  - 2. Conditional probability, independence, Bayes' theorem
  - 3. Integer random variables, expectation
  - 4. Law of large numbers

#### **Lab Activities**

No information provided

## **Objectives**

At the conclusion of this course, the student should be able to:

- Describe how formal tools of symbolic logic are used to model real-life situations, including those arising in computing contexts such as program correctness, database queries, and algorithms.
- 2. Relate the ideas of mathematical induction to recursion and recursively defined structures.
- 3. Analyze a problem to create relevant recurrence equations.
- 4. Demonstrate different traversal methods for trees and graphs.
- 5. Apply the binomial theorem to independent events and Bayes' theorem to dependent events

#### **Evaluation Methods**

Exams

Quizzes

**Programming Projects** 

**Discussions** 

#### Class Presentations

## **Textbooks**

Rosen (2006). *Discrete Mathematics and its Applications* (6th ed.). McGraw-Hill. [ISBN: 0071244743]

Descrete Mathematics. Richard Johnsonbaugh

Sipser (2005). *Introduction to the Theory of Computation* (2nd ed.). Course Technology. [ISBN: 0534950973]

Lipschutz and Lipson (2007). *Schaum's Outline Discrete Mathematics* (3rd ed.). McGraw-Hill. [ISBN: 0071470387]

Gaddis, Walters, and Muganda, *Starting out with C++: Early Objects*, 7th edition (ISBN-13: 978-0-13-607774-9)